ETG Scale Turbulence and Transport in the DIII-D Tokamak


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Abstract. Small-scale density turbulence \( k_{\perp}\rho_i \sim 4-10 \) and electron thermal transport are both observed to increase during electron cyclotron heating of a high temperature tokamak plasma \( k_{\perp} \) is the turbulent wavenumber and \( \rho_i \) the ion gyroradius). In contrast, large-scale turbulence \( k_{\perp}\rho_i \leq 1 \) and ion thermal transport remain effectively constant. This implies that the small-scale turbulence is not a remnant or tail of the ubiquitous, large-scale turbulence and also indicates a potentially important role in determining anomalous electron thermal transport.

1. Introduction

Energy and particle confinement observed in high-temperature tokamak fusion plasmas is often smaller than expected from collisional processes with the deficit attributed to transport arising from micro-instabilities or turbulence [1]. These instabilities include, but are not limited to, ion temperature gradient (ITG) driven modes \( k_{\perp}\rho_i \sim 0.1 \), trapped electron modes (TEM) \( k_{\perp}\rho_i \sim 1 \), and electron temperature gradient (ETG) driven modes \( k_{\perp}\rho_i \sim 10 \) where \( k_{\perp} \) is the fluctuation wavenumber perpendicular to the magnetic field \( B \) and \( \rho_i \) the ion gyroradius. Observations and simulations of low frequency, long wavelength fluctuations are consistent with such instabilities driving thermal and particle transport [1]. However, the current theoretical understanding regarding the role of high frequency, short wavelength modes is much less clear. Theory and simulation have predicted that such modes are capable of either driving significant [2,3] or little [4-7] electron thermal transport (note that Ref. [5] uses low magnetic shear which can affect the resulting transport levels). Experimental measurements are now beginning to attain the high wavenumbers necessary to address these issues [8-12]. Improved, unambiguous measurements across the wavenumber spectrum, particularly at high- \( k \), combined with simultaneous measurement of the transport properties are essential to elucidate understanding in this critical area.

In this paper, the response of both large and small-scale density fluctuations to auxiliary plasma heating in the form of electron cyclotron resonance heating (ECH) is described, together with the observed modifications in ion and electron thermal transport. It is found that while the large scale, low- \( k \) turbulence levels and ion thermal transport remain approximately constant during ECH, the high- \( k \) turbulence levels and electron thermal transport are observed to both increase. This indicates that the high- \( k \) fluctuations are not simply remnants of the large amplitude low- \( k \) turbulence often reported in the literature [e.g. 13,14]. The observations are also consistent with small-scale turbulence driving at least part of the electron heat transport, since no observed changes occur in the low \( k \) turbulence. Linear growth rate calculations for these plasmas using gyrokinetic simulation indicate large
increases (factors ~2-3) in the growth rates for low-\(k\) fluctuations across the majority of the plasma radius. Somewhat surprisingly, ECH is also found to locally reduce the radial electric field thereby increasing the electric field shearing rate over a broad plasma region. Current understanding of shear flow suppression of turbulence [15] suggests that the observed modification in the electric field profile serves to both constrain the growth of low-\(k\) fluctuation levels and modify the spectral characteristics in a manner consistent with observations.

2. Experiment and Results

Lower single-null plasmas with \(B_T = 1.9\) T, \(I_p = 700\) kA, and chord average density 1.5x10\(^{19}\) m\(^{-3}\) were used for the results reported here. ECH was initiated at 2000 ms with the injected power increased in a stepwise manner every 300 ms [Fig. 1(a)]. The power from the ECH was deposited in a radially localized volume centered at \(r/a = 0.6\pm0.1\) with maximum injected power of ~2.4 MW. The plasma electron temperature increased at all measured radii in a stepwise manner similar to the injected ECH [Fig. 1(c)]. In contrast, the ion temperature was not affected by the injected power while the electron density decreased by 10%-20% [Fig. 1(d)]. The decrease in electron density resulted in a change in the density profile shape discussed below. The thermal flux associated with ions and electrons was calculated based upon the ECH power deposition location and the measured profiles using the ONETWO transport code [16]. Two different times are shown in Fig. 2 corresponding to no ECH and 2.4 MW ECH power [times 1900 and 3100 ms in Fig. 1(a)]. As seen the ion energy flux did not change appreciably with ECH, consistent with the observed lack of variation in \(T_i\). In contrast, the electron energy flux increased significantly for \(r/a > 0.6\) between these two times. It is significant that the ECH dominantly affects the electron energy flux in this plasma parameter regime, having little effect on the ion energy flux.

![FIG. 1. (a) ECH heating, (b) neutral beam injection, (c) electron temperature at different radii showing increase with ECH, (d) chord average electron density and ion temperature.](image-url)
The behavior of the density fluctuations over a broad spectral range was monitored using far-infrared (FIR) scattering and millimeter (mm)-wave backscattering [17]. In addition, reflectometry and beam emission spectroscopy were also employed to locally investigate low-\(k\) density fluctuations. The FIR scattering system measures low-\(k\) density fluctuations possessing a nearly poloidal wavenumber. The scattered signal is integrated over the wavenumber range 0-2 cm\(^{-1}\) with the signal originating from a chord oriented radially along the plasma midplane. The high-\(k\) mm-wave backscatter system monitors density fluctuations with a predominately radial wavenumber in the range \(k = 35-39\) cm\(^{-1}\). For the plasmas discussed here this corresponds to a normalized wavenumber range of \(k_{\parallel}\rho_i \sim 0-0.6\) and \(k_{\perp}\rho_i \sim 4-10\) for the low and high \(k\) ranges respectively. The high \(k\) signal originates from a chord lying near the midplane which begins at the outboard edge and ends on the low field side at \(\rho \approx 0.4\).

During the high power ECH, low-\(k\) fluctuations (\(k_0 \sim 0-2\) cm\(^{-1}\), from FIR scattering) were observed to decrease in spectral width [Fig. 3(a)] while the integrated normalized amplitude \(\tilde{n}/n\) remained approximately constant [Fig. 3(b)]. In contrast to this behavior, the high-\(k\) fluctuations increase both in frequency width and normalized amplitude \(\tilde{n}/n\) during ECH [Fig. 3(c,d)]. The increase in the high-\(k\) RMS turbulence level is approximately 35% comparing the two times 1975 and 3100 ms. This very different response indicates that the high \(k\) turbulence evolves independently of the lower \(k\) ITG/TEM-like turbulence often observed in tokamak plasmas. In addition, the fact that high \(k\) turbulence increases simultaneously with the observed increase in electron energy transport indicates a potentially important role in determining anomalous electron thermal transport. This strongly motivates the continued pursuit of such measurements along with detailed comparisons to nonlinear gyrokinetic calculations.
FIG. 3. Low $k$ frequency spectra narrow (a) and normalized fluctuation levels $\tilde{n}/n$ (b) are constant or decrease during ECH. In contrast, high $k$ spectra broaden (c) and fluctuation levels $\tilde{n}/n$ (d) increase. Note that the low $k$ data is heterodyne and therefore shows the propagation direction of the fluctuations while the high $k$ data is homodyne and so shows no information on the direction of propagation.

3. Experiment-Theory Comparisons

In order to compare experimental observations with theoretical expectations, calculations have been performed using the linear gyrokinetic stability code GKS [18]. These calculations indicate that the discharges described in this paper were unstable to a wide range of instabilities: ETG, ITG and TEM. GKS is a gyrokinetic stability code which calculates linear growth rates and frequencies for toroidal drift waves corresponding to poloidal wavenumbers. Code inputs are the measured $T_e$, $T_i$, $n_e$, and $Z_{\text{eff}}$ profiles, and magnetic equilibrium. It does not include the effects due to up-down plasma asymmetries or $E\times B$ velocity shear flow ($E$ and $B$ are local electric and magnetic fields). Radial profiles of temperature and density for the two times of interest are shown in Fig. 4(a,b). Fig. 1 shows that the electron temperature increases significantly across the whole radius while the ion temperature remained constant. The electron density decreased everywhere except at the very edge. The value of these parameters and their scale lengths are significant inputs into calculations (both analytic and numerical) of various plasma instabilities.

FIG. 4. (a) Ion and electron temperature and (b) density profiles from two times: Ohmic and ECH heating.
Figure 5(a,c) shows the growth rates $\gamma$ over the radial range $\rho = 0.1-0.9$ for values relevant to the measured data shown in Fig. 3(a,b) ($\gamma > 0$ indicates instability). It is seen that the plasma is unstable over a range in wavenumber and real space. From Fig. 5(a) it is seen that the low-$k$ growth rate increases significantly during ECH whereas experimentally no change in the fluctuation level was observed [Fig. 3(b)]. Also an increase in real frequency [Fig. 5(b)] is predicted for low $k$ whereas in the experiment a narrowing of the low-$k$ turbulent frequency spectrum was observed. The high-$k$ growth rate increases for $r/a > 0.85$ but decreases towards the interior. The increased real frequency [Fig. 5(d)] is similar to the observed increase in high-$k$ spectral bandwidth [Fig. 3(c)]. Shown in Fig. 6 are the experimental temperature scale lengths compared to the calculated critical gradient [19] for ETG modes. The experimental gradient is larger than the calculated ETG critical gradient over a large radial range indicating that the calculated high $k$ growth rates [Fig. 5(c)] are consistent with ETG type modes.

![Figure 5](image1.png)

**FIG. 5.** GKS predictions of growth rates and real frequencies for two different wavenumbers (a,b) $1 \text{ cm}^{-1}$ and (c,d) $35 \text{ cm}^{-1}$ for two times: Ohmic (solid line) and ECH (dotted line) heating.

![Figure 6](image2.png)

**FIG. 6.** Comparing theoretical ETG critical gradient predictions with experimental gradients. The critical gradient is exceeded for most of the outer half radius in both heating conditions.
Previous theoretical and experimental work indicates that radial electric field shear can lead to significant changes in fluctuations levels and transport [15]. In the experiments here the radial electric field is strongly modified by the ECH where a change is observed for r/a > 0.4 [Fig. 7(a)]. The effect of the ECH is to decrease $E_r$ and to increase the electric field shear around the regions r/a ~ 0.5 and r/a ~ 0.9. The net effect of the reduced electric field strength is to decrease the $E \times B$ velocity Doppler shift of fluctuations as observed in the laboratory reference frame. This agrees well with the observed narrowing in the low-k turbulence frequency spectrum shown in Fig. 3(a). As reviewed in Ref. 15 there is significant evidence that electric field shear can affect low k fluctuations if the shearing rate $\gamma_{E \times B}$ due to shear $E \times B$ velocity flow is a significant fraction of the linear growth rates. Figure 7(b) shows that the shearing rate $\gamma_{E \times B}$ increases over an extended spatial region during ECH. This suggests that the predicted increase in low-k turbulence growth rate may be offset by the increased ExB shearing rate.

![FIG. 7. (a) Electric field and (b) shear shown during Ohmic and ECH time periods. modified by ECH. Typical uncertainties are shown by the vertical bars in (a) and (b).](image)

### 4. Summary and Conclusion

In summary, high wavenumber ($k \rho_i = 4-10$) or electron temperature gradient (ETG) scale plasma turbulence increases in normalized amplitude $\tilde{n}/n$ in the outer plasma region and spectrally broadens during ECH heating of DIII-D Ohmic plasmas. This correlates with an observed increase in electron heat flux in the outer plasma region. In contrast, turbulence at low wave numbers was observed to remain approximately constant in normalized amplitude $\tilde{n}/n$ while the frequency spectrum narrowed. The implication of these observations is that the high-k turbulence evolves independently of the lower-k turbulence. Linear growth rate calculations at low-k indicate increases across a broad spatial region during ECH in disagreement with the observed minor modifications in low-k turbulence levels. However, changes in electric field strength and electric field shear are also observed during ECH. These changes provide an explanation for the observed spectral narrowing at low-k and provide a plausible regulation mechanism (i.e. increased damping due to sheared $E \times B$ velocity tends to offset the increased low-k growth rates). It should be noted that $E \times B$ shearing is not expected to play an important role at small turbulent scales [3] where a significant increase is observed in the experiment.

The results presented in this paper are important especially since recent theoretical work has not fully concluded what role, if any, small-scale turbulence ($k \rho_i > 4$) plays in governing
anomalous electron thermal transport. The data presented indicate that high-$k$ turbulence could contribute to electron heat transport in the studied plasmas motivating expansion of such measurements along with detailed comparisons to nonlinear gyrokinetic calculations.

This work was supported by the U.S. Department of Energy under DE-FG03-01ER54615, DE-FC02-04ER54698, DE-AC05-76OR00033, DE-FG02-89ER53296, and SC6832401.

References